Modeling and Querying Multidimensional Bitemporal Data Warehouses

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Abstract: Data warehouses have been considered to be the key aspect of success for any Decision Support System (DSS). Temporal database research has produced important results in this field. Data warehouses store historical data, and therefore could clearly benefit from the research on temporal databases. Temporal data warehouses join the two fields of temporal databases and data warehouse research. This paper introduces a bitemporal data warehouse model that both valid time and transaction time are attached to attributes. Data warehouse objects and cubes are created with multidimensional bitemporal relational database. Performance of available well-known relational database and bitemporal extension for data warehouse is evaluated and compared in terms of execution time and disk space consumption with the set of queries.

Key words: Attribute time stamping, big data, bitemporal databases, data warehouse, OLAP.

1. Introduction

Big data is one of the most popular research topics in recent years. Technology is an indispensable part of people's life. Communication, shopping, transaction habits have changed. When surfing on social web sides a lot of data is left unconsciously. This data is processed and utilized to make recommendations or utilized to increase profits.

Data warehousing has been an active research area, with the purpose to access historical data. A data warehouse is "a collection of subject-oriented, integrated, non-volatile, and time-variant data to support management's decisions" [1]. It attempts to obtain specially prepared data in an easy and quick way. This type of data is used in management reports, various business queries, decision support systems, manager information systems, and data mining applications all by linking the various silos of data that are distributed throughout an organization [2]. From the early nineties, data warehouses have been considered to be the key aspect of success for any Decision Support System (DSS). Undoubtedly, the user of a data warehouse needs to be confident that the data in that warehouse is timely, accurate, and complete. Non-volatile and time-variant data features of data warehousing suggest that it should allow changes to data values without overwriting existing values.

OLAP (online analytical processing) is an outgrowth of the need to reach live, real, and prepared data. It is possible to perform future analysis with OLAP reports with good statistical reliability. The data in an OLAP cube is updated and worked out again at certain times of the day. Totals, averages, and the other operations

are calculated over with this new live data. When a report is presented via OLAP cubes, there is no calculation performed when reporting. All the calculated values are generally stored in the OLAP cubes as before. The only processing consists of calling the report and then displaying it. Versioning and dynamic update of OLAP dimensions are studied in [3], [4]. Typical OLAP operations include rollup (increasing the level of aggregation) and drill-down (decreasing the level of aggregation or increasing detail) along one or more dimension hierarchies, slice_and_dice (selection and projection), and pivot (re-orienting the multidimensional view of data) [5], [6].

Temporal database research has produced important results in this field. A temporal database may capture either the history of the relevant objects and their attributes (known as valid time), or the history of the database activity (known as transaction time). A valid time is necessarily used in order to model the time-varying states of an object and its attributes. These states may be in the past, present, or even in the future. A transaction time denotes the timestamp of any change as it is recorded in the database. It may not extend beyond the current time and is system generated. Having only a valid time captures the history of an object, but it does not preserve the history of any retroactive or post active changes. Having only the transaction time, one does not preserve the historical or future data, i.e., the validity period of data values. However, bitemporal databases can model our changing knowledge of a changing world, and hence associate data values with facts, and thus specify when the facts were valid, thereby providing a complete history of the data values and their changes [7].

Data warehouses store historical data, and therefore could clearly benefit from the research on temporal databases. Temporal data warehouses join the two fields of temporal databases and data warehouse research, in order to manage time-varying multidimensional data. There are research projects that have already combined data warehouses and temporal databases. A multidimensional model is presented by Malinowski and Zimanyi [8] that allows time varying and time-invariant examples. Martin and Abello [9] introduced detailed information about differences and similarities between data warehouse and temporal database. Eder, Koncilia and Morzy [10] implemented temporal data warehouse model with two different approach. One of them is called direct approach which uses a query analyzer and result analyzer to obtain the result of each. Other one is called indirect approach that generates a data mart for a particular structure version and transforms the data from all other structure versions into this data mart using the given specication of transformation functions. While the direct approach offers greater flexibility, the indirect approach is superior in terms of response time, once the data mart has been generated. Janet, Ram'irez and Guerrero [11] present a model for changing, adding, removing dimensions of data warehouse cube with no harmful affect to current applications as well as a query language to manage multidimensional schemas. Combi, Oliboni and Pozzi [12] present a graph-based model for temporal semi structured data warehouses also a query language to get required information usefully.

In this paper, we propose a bitemporal extension for data warehouse and OLAP applications in which both valid time and transaction time are attached to attributes. There are research projects that have already combined data warehouses and temporal databases. Nonetheless, all of them considered the tuple time-stamped temporal database approach. To the best of our knowledge, the combination of data warehousing and attribute time stamping has not been studied before.

The rest of the paper is organized as follows. Section 2 outlines bitemporal databases and common two time stamping approaches. In Section 3, brief information outlined about data warehouses. Section 4 presents proposed model for bitemporal data warehouses and implementation details. In Section 5 we present sample queries and test results for the empirical study. Section 6 presents our conclusion and plans for future work.

2. Bitemporal Databases

Historical database offers temporal knowledge about objects but do not contain system modifications. Transaction database offers system changes but do not contain temporal information about objects. Historical and transactional databases must be combined to have complete information about objects. Bitemporal database covers both these requirements. In this manner, bitemporal databases demonstrate real world's data according to real time [13]-[16].

There are two common approaches as to how temporal databases can be implemented: 1) tuple time-stamping, which uses first normal-form (1NF) relations, and 2) attribute-value time-stamping, which requires non-first normal-form (N1NF) relations. In the case of tuple time-stamping, a separate relation is required for each time dependent attribute unless they change simultaneously. Non-time-varying attributes are grouped into a different relation. A relation scheme is augmented with two (four) time attributes to designate the time reference of its tuples. Tuple time stamping uses all of the advantages of traditional relational databases. However, each time varying attribute should be in a separate relation, which results in many small relations. Validity period of product's list price is the time period between valid time lower bound (VT_LB) and valid time upper bound (VT_UB). If a record is valid in current time VT_UB value is set to 'now'. In addition, all the previous and the current list price transaction time lower bound (TT_LB) and transaction time upper bound (TT_UB) are stored. An item MB1's list price was 1191.17 and transaction time lower bound stored as 24.09.2002. When the item MB1's value has changed to 1226.9 on 01.07.2002 VT_UB column changed and new tuple is inserted. This information is stored into the system on 02.07.2002, as illustrated in Table 1.

 Table 1. Tuple Time Stamped Bitemporal Approach

P. Name	Color	List Price	VT_LB	VT_UB	TT_LB	TT_UB
MB1	Black	1191.17	25.09.2001	01.07.2002	24.09.2001	01.07.2002
MB1	Black	1226.9	02.07.2002	now	02.07.2002	now
MB2	Yellow	120.43	18.10.2002	now	20.10.2002	now
MP	Red	150	30.07.2002	now	01.08.2002	now
MA	Black	35.89	18.10.2002	now	20.10.2002	now

In the case of attribute time-stamping, N1NF relations are used, and timestamps are attached to attribute values. Entire data about an object being modeled can be stored in one tuple of the N1NF relation. The history of values is stored separately for each attribute and the entire history of an object is stored in one tuple. Thus, values in a tuple that are not affected by an update do not have to be repeated. All time-varying attributes can be modeled in one relation. This relation may have non-time-varying attributes along the time dependent attributes.

A Bitemporal atom [7] is defined as a triplet, <valid time, transaction time, value>, where the valid and transaction time components can be applied as a time point, a time interval, or a temporal element. A Bitemporal atom in the form of <[VTl, VTu), [TTl, TTu), V> represents Valid time lower bound (VT_LB), Valid time upper bound (VT_UB) ,Transaction time lower bound (TT_LB), Transaction time upper bound (TT_UB) and Data value, respectively.

The bitemporal atom {<[25.09.2001, 01.07.2002], [24.09.2001, 01.07.2002], 1191.17>, <[02.07.2002, now], [02.07.2002, now], 1226.9>} in Table 2 states that product MB1 was written to the database at transaction time 24.09.2001, effective starting from valid time 25.09.2001. Approximately ten months later, when transaction time was 01.07.2002, product MB1's price has increased to 1226.9 valid from the same day. When an update operation is performed, a new row is added to only 'List Price' attribute, other attributes are not affected.

P. Name	Color	List Price
MB1	Black	{<[25.09.2001, 01.07.2002], [24.09.2001, 01.07.2002], 1191.17 >, <[02.07.2002, now], [01.07.2002, now], 1226.9>}
MB2	Yellow	<[18.10.2002, now], [20.10.2002, now], 120.43>
MP	Red	<[30.07.2002, now], [01.08.2002, now], 150>
MA	Black	<[18.10.2002, now], [20.10.2002, now], 35.89>
TR	Black	<[30.07.2002, now], [01.08.2002, now], 22.11>

Table 2. Attribute Time-Stamped Bitemporal Approach

3. Data Warehouses

The schema of a data warehouse lies on two kinds of elements: facts and dimensions. Facts are used to memorize measures about events. Dimensions are used to analyze these measures, through counting, summation, average, etc. We will explain these ideas by the analysis of the list price of a product according to the product category and product model. Each list price of a product is a fact which is characterized by a quantity. Subcategory and model are criterions of the dimension Product. A quantity is so connected both with a type of product. This type of connection concerns the organization of facts with regard to dimensions. The possibilities of fact analysis depend on these two forms of connection and on the schema of the warehouse. This schema is chosen by the designer in accordance with the user's needs. Determining the schema of a data warehouse is achieved with adequate modeling of dimensions and facts. To facilitate visualization and complex analyses, the data in a warehouse is typically modeled multidimensionality. Multidimensional modeling represents data as points in multidimensional space. Fig. 1 depicts a cube representation used in the multi- dimensional context which list prices are analyzed according to product, model and subcategory.



Fig. 1. Cube representation of the multidimensional model.

A main fact table is used when designing a cube. This fact table contains summarized measures by means of the cube's dimensions. Fact table is related to dimension tables that are formed from facts like model, category and product dimensions. Often, these dimensions are hierarchical; product may be organized as a product-category-industry hierarchy. For instance category table's dimension levels can be Bikes, Components, Clothing and Accessories. These levels contain an attribute of dimension tables in which better reporting is provided. The data and metrics in fact table can be summarized in 1, 2, 3, 4 dimensional cubes.

4. Bitemporal Data Warehouse Model and Implementation

We obtained data from the Microsoft Adventure Works (AW) database that is available to the public for research and experiment purposes. Although said database has five modules, we only applied our method to the Production module. We reformed the Production module schema as nested attribute time-stamped bitemporal schema. According to the AW structure, some tables are built in their related tables as nested tables to avoid redundancy. Whereas there are 25 tables in the AW database Product module, our method generated 15 tables.

The type system facilities of object-relational databases allow us to define a bitemporal atom as a structured user defined type as seen in Fig. 2. Removing or retrieving a component such as the transaction time lower and/or upper bound is allowed and used in the query expressions. Once the user defined type is defined, it can be used in SQL statements where other built-in types are used.

CREATE TYPE BT_NUMBER AS (
VT_LB DATE,
VT_UB DATE,
TT_LB DATE,
TT_UB DATE,
VALUE NUMBER);

Fig. 2. User defined type definition of a bitemporal atom BT_NUMBER.

CREATE TYPE LISTPRICE AS TABLE OF BT_NUMBER; CREATE TYPE PRODUCTSELL AS TABLE OF BT_NUMBER; CREATE TYPE PRODUCTCOST AS TABLE OF BT_NUMBER;

Fig. 3. The tuples of LISTPRICE are as nested table, BT_NUMBER.

User Defined Types can be declared to be the "data type" of an entire table such that the table's attributes are defined by the User Defined Type. By in-lining the repeated fields in the table, the reliance on creating another table with its own structure and indexes is removed in collection type tables. Data manipulation operations such as select, insert, and delete can be applied similar to ordinary tables. A nested table is an unordered collection of elements of the same data type. It can have any number of elements; no maximum number is specified in the definition of the table.

A tuple in a nested bitemporal relation is an instance of the structured type on which the table is defined. It gives the instance a unique identity. Having a set of identical User Defined Types in a single tuple actually simulates the attribute time-stamping approach with a single-attribute table for each object's time related attributes.

The AW database table structure and temporal construction is analyzed and re-designed. The SQL statement in Fig. 3 shows that LISTPRICE, PRODUCTSELL, and PRODUCTCOST are attribute time-stamped bitemporal relations. These bitemporal tables are single-attribute tables with a type of BT_NUMBER. The table can have as many tuples as required to represent bitemporal atoms.

Conceptual models allow describing the requirements of an application in terms that are as close as possible to users' perception. Thus, they facilitate the communication between users and designers since they do not require the knowledge of technical features of the underlying implementation platform [8]. The conceptual model for the proposed Multidimensional Bitemporal Data Warehouse is shown in Fig. 4.



Fig. 4. Multidimensional bitemporal data warehouse conceptual model.

A fact table is connected to three or more dimension tables. A dimension is composed of one or more hierarchies, whereas each hierarchy belongs to only one dimension. A hierarchy contains one or more related levels that can be shared between different hierarchies. Levels have a key and descriptive attributes. Attributes have a name and a type, which must be a data type, i.e., integer, real, string, etc. Bitemporal support for levels and for attributes is captured by the multivalued attribute of type BT_NUMBER. A hierarchy is temporal if it has at least one temporal level. A dimension is temporal if it has at least one temporal hierarchy. Levels, hierarchies, and dimensions can have many time-varying attributes stored as nested tables.

After analyzing the AW database, we designed five cubes; Product, ProductListPrice, ProductCostHistory, ProductCost History2Dim, ProductListPrice2Dim and Workorder_Order- Qty from the Production module. The fact table Cube_ Product_ListPrice contains the attributes D1_Unitmeasure, D2_Subcategory, and D3_Product MDC foreign keys from three dimensions, and the LISTPRICE type of BT_NUMBER as illustrated in Fig. 5.

The Cube_Product_ListPrice fact table is formed by three dimensions; Dim_Model, Dim_UnitMeasure and Dim_- Subcategory. The Dim_Model dimension table contains Dimension_Key attribute as a primary key and attributes Model_Min_Cost and Model_Number are type of BT_NUMBER. The Dim_UnitMeasure dimension table contains Unitmeasure_Id attribute as a primary key and Unitmeasure_Number is type of BT_NUMBER. The Dim_Subcategory dimension table contains Dimension_Key attribute as primary key, Subcategory_Min_Cost is type of BT_number. The Dim_Subcategory has a level named Subcategory that has an attribute Subcategory_Number data type of BT_NUMBER. Level_Category contains Category_- Number type of BT_NUMBER as presented in Fig. 5.



Fig. 5. A snowflake schema based on Cube_Product_ListPrice table.

5. Queries for Bitemporal Data Warehouse

In order to demonstrate the feasibility of our proposed model, we ran queries for both original relational tables and multidimensional bitemporal data warehouse cubes. We also displayed OLAP and SQL query

codes written for both approaches as illustrated in Tables 3 to 6. Each query was run six times and the average value is selected. Fig. 6 is the result of query times for all queries.

5.1. Query 1: What Is the Average List Price of Bikes According to Years?

The Query 1 is written for both the multidimensional bitemporal data warehouse cubes and the relational database tables as illustrated in Table 3. The multidimensional bitemporal data warehouse script retrieves result from CUBEPRODUCTLISTPRICE table and contains one nested select statement that retrieves data from DIM_SUBCATE- GORY dimension table. The relational database script retrieves data from PRODUCTLISTPRICE- HISTORY table and contains three nested select queries, each of these nested select queries retrieve data from separate tables.

Table 3. Query 1 with Multidimensional Bitemporal and Relational Databases

Multidimensional Bitemporal:

SELECT AVG(LISTPRICE.VALUE), LISTPRICE .VT_LB, LISTPRICE.VT_UB, LISTPRICE.TT_LB **FROM** CUBEPRODUCTLISTPRICE **WHERE** DIM_SUBCATEGORY_KEY IN (**SELECT** DIMENSION_KEY **FROM** DIM_SUBCATEGORY **WHERE** CATEGORY_NAME='BIKES') **GROUP BY** VT_LB ,TT_LB;

Relational:

SELECT AVG(LISTPRICE), STARTDATE, ENDDATE, MODIFIEDDATE **FROM** PRODUCTION.PRODUCTLISTPRICEHISTORY**WHERE** PRODUCTID IN (**SELECT** PRODUCTID **FROM** PRODUCTION.PRODUCT **WHERE** PRODUCTSUBCATEGORYID IN (**SELECT** PRODUCTSUBCATEGORYID **FROM** PRODUCTION.PRODUCTSUBCATEGORY **WHERE** PRODUCTCATEGORYID= (**SELECT** PRODUCTCATEGORYID **FROM** PRODUCTION.PRODUCTCATEGORY **WHERE** NAME='BIKES'))) **GROUP BY** STARTDATE, MODIFIEDDATE;

5.2. Query 2: What Is the Average List Price of Bikes According to Cultures?

Scripts that give the same result for the Query 2 is written for the multidimensional bitemporal data warehouse cube tables and the relational database tables as depicted in Table 4 The multidimensional bitemporal data warehouse script retrieves result from CUBEPRODUCTLISTPRICE cube and DIM_MODEL dimension tables, associated each other by a where clause. The multidimensional bitemporal datawarehouse script contains two nested select statements to retrieve data from separate tables. The relational database script retrieves data from four separate tables, associated each other by five where clauses.

Table 4. Query 2 with Multidimensional Bitemporal and Relational Databases

Multidimensional Bitemporal:
SELECT AVG(LISTPRICE) AS AVERAGE_BIKE_PRICE, DIM_MODEL.CULTURE_NAME
FROM CUBEPRODUCTLISTPRICE, DIM_MODEL WHERE DIM_MODEL.DIMENSION_KEY=
CUBEPRODUCTLISTPRICE.DIM_PRODUCTMDC_KEY AND CUBEPRODUCTLISTPRICE.PRODUCT_ID
IN (SELECT PRODUCTID FROM PRODUCT2 WHERE SUBCATEGORYID
IN (SELECT SUBCATEGORY_ID FROM DIM_SUBCATEGORY WHERE CATEGORY_NAME='BIKES'))
GROUP BY DIM_MODEL.CULTURE_NAME ORDER BY DIM_MODEL.CULTURE_NAME;
Relational:
SELECT AVG(PL.LISTPRICE) AS AVERAGE_BIKE_PRICE, C.NAME
FROM PRODUCTION.PRODUCTLISTPRICEHISTORY PL, PRODUCTION.PRODUCTMODEL PM, PRODUCTION.PRODUCT P,
PRODUCTION.PRODUCTMODELPRODUCTDESCRIPTIONCULTURE PMDC , PRODUCTION.CULTURE C
WHERE P.PRODUCTMODELID=PM.PRODUCTMODELID AND PL.PRODUCTID=P.PRODUCTID
AND PM.PRODUCTMODELID=PMDC.PRODUCTMODELID AND PMDC.CULTUREID=C.CULTUREID)
AND PL.PRODUCTID IN (SELECT PRODUCTID FROM PRODUCTION.PRODUCT
WHERE PRODUCTSUBCATEGORYID IN (SELECT PRODUCTSUBCATEGORYID
FROM PRODUCTION.PRODUCTSUBCATEGORY WHERE PRODUCTCATEGORYID=
(SELECT PRODUCTCATEGORYID FROM PRODUCTION.PRODUCTCATEGORY
WHERE NAME='BIKES'))) GROUP BY C.NAME ORDER BY C.NAME;

5.3. Query 3: What Is the Average List Price of Components According to Cultures and Models?

The Query 3 for the multidimensional bitemporal data warehouse retrieves data from CUBEPRODUCTLISTPRICE cube and DIM_MODEL dimension tables. It contains two nested select statements. The relational database code retrieves data from four separate tables that contains three nested select queries as seen in Table 5.

Table 5. Query 3 with Dimensional and Relational Databases

GROUP BY C.NAME, PM.NAME ORDER BY C.NAME, PM.NAME;

5.4. Query 4: List of All Work Orders in Ordered by According to Category, Subcategory and Product Name.

The multidimensional bitemporal data warehouse query retrieves data from CUBE_WORKORDER_ORDERQTY cube and DIM_PRODUCT dimension tables associated each other by a where clause. The relational database query retrieves data from four separate tables as illustrated in Table 6.

Table 6. Query 4 with Multidimensional Bitemporal and Relational Databases

Multidimensional Bitemporal:

SELECT CUBE_WORKORDER_ORDERQTY.VT_LB, CUBE_WORKORDER_ORDERQTY.VT_UB,

CUBE_WORKORDER_ORDERQTY.TT_LB, CUBE_WORKORDER_ORDERQTY.TT_UB, CUBE_WORKORDER_ORDERQTY.VALUE ORDERQTY, DIM_PRODUCT.CATEGORY_NAME, DIM_PRODUCT.SUBCATEGORY_NAME, DIM_PRODUCT.PRODUCT_NAME **FROM** CUBE_WORKORDER_ORDERQTY, DIM_PRODUCT

WHERE DIM_PRODUCT.DIMENSION_KEY= CUBE_WORKORDER_ORDERQTY.DIM_PRODUCT_KEY

ORDER BY DIM_PRODUCT.CATEGORY_NAME, DIM_PRODUCT.SUBCATEGORY_NAME, DIM_PRODUCT.PRODUCT_NAME;

Relational:

SELECT WO.STARTDATE, WO.ENDDATE , WO.MODIFIEDDATE, WO.MODIFIEDDATE, WO.ORDERQTY, PS.NAME, PC.NAME, P.NAME **FROM** PRODUCTION.WORKORDER WO,

PRODUCTION.PRODUCT P, PRODUCTION.PRODUCTSUBCATEGORY PS, PRODUCTION.PRODUCTCATEGORY PC **WHERE** P.PRODUCTID=WO.PRODUCTID AND P.PRODUCTSUBCATEGORYID=PS.PRODUCTSUBCATEGORYID AND PS.PRODUCTCATEGORYID=PC.PRODUCTCATEGORYID **ORDER BY** PS.NAME, PC.NAME, P.NAME



Fig. 6. Execution times for all queries.

The multidimensional bitemporal model is designed with user-defined types and nested relations; therefore it requires fewer tables in queries as depicted in Tables 3 to 6. On the other hand, relational tables join more tables, which mean more disk reads to execute queries. Consequently, the relational database requires more time in queries as illustrated in Fig. 6. It is also interesting to observe that the multidimensional bitemporal tables acquired 11,392 Kb and relational tables captured 34,688 Kb in segments. The latter approach requires three times more memory than the first approach for the same data.

6. Conclusion

Data warehousing is closely related to customer relationship management (CRM) systems, global e-commerce enterprises, supply chain management (SCM), enterprise resource planning (ERP) systems, corporate information portals, and strategy management informatics. Progressively, data warehousing becomes an integral part of the aforementioned systems.

In this study, we proposed a bitemporal extension of the data warehouse model that supports valid time and transaction time on the attribute level and completed empirical implementation. Our model allows the representation of any changes to transaction and valid data. Furthermore, it enables our databases to model our changing knowledge of a changing world, and hence associate data values with facts and specify when the facts were valid, thereby providing a complete history of data values and their changes. In order to accurately and completely model the real world, both time dimensions are needed.

We evaluated the performance of implementation method to gain insight into its relative performance. Results show that proposed model ensures better outcome and better performance.

Many companies use data warehousing technologies to get more effective and faster reports. The attribute time-stamped bitemporal approach performs less join statement and less background operations in data warehouse. Therefore, data warehousing reports are achieved in higher performance. It is our hope that our work will lay the foundation for the implementation of data warehouses.

For the future work, data warehouse may be analyzed according to different time intervals with the flexibility of bitemporal structure. Purchasing habits of customers may be analyzed in time line. The efficient periods of year can be figured out. These and similar beneficial conditions may be analyzed faster than the other systems, together with the benefits of data warehouse and user defined types and nested table data storage. Outcomes will help corporates for determining their strategy.

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