# Frequency-Dependent Smith-Chart Model as Applied to Integrated Circuit Package Antenna Design

Settapong Malisuwan and Jesada Sivaraks

Abstract—In this paper, the frequency-dependent Smith-Chart representation is utilized to improve the accuracy of integrated circuit package antenna (ICPA) design. The purpose of this research is to reveal that the frequency-dependent Smith-Chart method (FDSC) is more exact than alternative models adopted in past research. The results in this research show that the FDSC model is more accurate than the previous model in the literature by comparing to the measure results. The method utilized in this paper can be applied to use in CAD applications with fast and user-friendly implementations.

Index Terms—Frequency dependent, Smith-chart, ICPA, CAD.

#### I. INTRODUCTION

The Smith-chart is an exceptional graphical tool used in high-frequency engineering to design amplifiers, filters, circuits and other impedance and reflection coefficient charts. Although there are other tools adopted to design components aforementioned, the Smith-chart is vastly known and is the most popular tool amongst them. It is a significant tool used in modern computer-aided design software (CAD) for high frequency designs.

The frequency-dependent Smith chart (FDSC) was proposed in [1], [2]. The results in [1], [2] suggests that FDSC gives more accurate results than the models adopted in past literature [3]. Basically in FDSC, the frequency-dependent characteristic impedance is addressed in higher detail in included in the algorithm hence risk of possible error is reduced. The purpose of this paper is to present the accuracy of FDSC model to design the ICPA.

In the next sections, the FDSC representation is explained and utilized to design the microstrip patch antenna and ICPA circuit.

## II. FREQUENCY-DEPENDENT SMITH-CHART REPRESENTATION

In this section, we describe the concept of FDSC model prior to apply the concept to design the ICPA circuit to achieve the objective.

The concept of microstrip-based Cole-Cole diagram is adopted to create a frequency-dependent (lossy) Smith-chart

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to scrutinize microstrip line characteristics [1]. Prior to analyzing the frequency-dependent Smith-chart variables, the capacitance parameter in microstrip-line system should be analyzed. The capacitance per unit length of the classical parallel-plate capacitor is [4]:

$$C = \varepsilon \frac{w}{h} \tag{1}$$

A simple frequency-dependent capacitance of the parallel-plate capacitor can be expressed in any frequency-dependent attributes of  $\varepsilon$  which is

$$C(\omega) = \varepsilon_0 \varepsilon^*(\omega) \frac{w}{h}$$
<sup>(2)</sup>

where  $\varepsilon^*(\omega)$  is a complex permittivity is expressed as  $\varepsilon'(\omega) - j\varepsilon''(\omega)$ .

Therefore,

$$C(\omega) = \varepsilon_0 \varepsilon'(\omega) \frac{w}{h} - j\varepsilon_0 \varepsilon''(\omega) \frac{w}{h}$$
(3)

Referring to the equivalent Cole-Cole diagram deduced for a parallel-plate microstrip line in [3] is substitute into Eqn. (3). Hence,

$$C(\omega) = C\left(\frac{1}{1+Q(\omega)} \left[Q(\omega) + \frac{\varepsilon_{eff}(0)}{\varepsilon_r}\right]\right) - j\frac{C}{\varepsilon_r} \left[\varepsilon_u^{"}(\omega) + \varepsilon_c^{"}(\omega) + \varepsilon_d^{"}(\omega)\right]$$

$$(4)$$

where  $C = \varepsilon_0 \varepsilon_r (w/h)$ .

For simplicity, the coefficients of Eqn. (4) are defined as follows:

$$A(\omega) = \frac{1}{1 + Q(\omega)} \left[ Q(\omega) + \frac{\varepsilon_{eff}(0)}{\varepsilon_r} \right]$$
(5)

$$B(\omega) = \frac{1}{\varepsilon_r} \left[ \varepsilon_u^{"}(\omega) + \varepsilon_c^{"}(\omega) + \varepsilon_d^{"}(\omega) \right]$$
(6)

In general, the characteristic impedance of a transmission line is given by:

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$$Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}}$$
(7)

where R, L, G, C are per unit length quantities defined as follows:

R = resistance per unit length in  $\Omega/m$ .

L = inductance per unit length in H/m.

G =conductance per unit length in S/m.

C = capacitance per unit length in F/m. [1]

If G and C are neglected, the characteristic impedance can be written as:

$$Z_0 = \sqrt{\frac{L}{C}}$$
(8)

To achieve frequency-dependent characteristic impedance  $(Z_0'(\omega))$ , the frequency-dependent capacitance  $(C(\omega))$  of Eqn. (4) is replaced into the capacitance (C) in Eqn. (8).Therefore, frequency-dependent characteristic impedance is

$$Z'_{0}(\omega) = \sqrt{\frac{L}{C[A(\omega) - jB(\omega)]}} = \frac{Z_{0}}{\sqrt{A(\omega) - jB(\omega)}}$$
(9)

Now, the frequency-dependent (lossy) Smith-chart can be derived through input of  $Z'_0(\omega)$  in Eqn. (9) into the normalized terminal impedance expression as done in traditional Smith-chart model [5]. Therefore the normalized terminal impedance  $Z'_L$  is

$$Z'_{L} = \frac{Z_{L}}{Z'_{0}(\omega)} = br + jbx \quad (Dimensionless)$$
(10)

As *r* and *x* are the normalized resistance and normalized reactance, and  $b = \sqrt{A(\omega) - jb(\omega)}$ .

The voltage reflection coefficient of present Smith chart is

$$\Gamma' = \Gamma_r' + j\Gamma_i' = \frac{Z_L' - 1}{Z_L' + 1}$$
(11)

or

$$Z'_{L} = \frac{Z_{L}}{Z'_{0}(\omega)} = br + jbx = \frac{(1 + \Gamma'_{r}) + j\Gamma'_{i}}{(1 - \Gamma'_{r}) - j\Gamma'_{i}}$$
(12)

Now, the set of equations representing the modified Smith-chart is expressed as:

$$\left(\Gamma_{r}' - \frac{br}{1+br}\right)^{2} + {\Gamma_{i}'}^{2} = \frac{1}{(1+br)^{2}}$$
(13)

and

$$(\Gamma_{r}^{'}-1)^{2} + \left(\Gamma_{i}^{'}-\frac{1}{bx}\right)^{2} = \left(\frac{1}{bx}\right)^{2}$$
(14)

As mentioned earlier in this paper, the objective of this research is to utilize the FDSC model to design the ICPA. To present the accuracy of the FDSC model, this paper uses the characteristics of the ICPA circuit from [6] to construct the FDSC diagram to meet this specific case [6].

The FDSC diagram is compared with a standard Smith-Chart in Fig. 1.

It can be seen that when the lossy characteristics (substrate loss, conductor loss, and frequency-dependent characteristic impedance of the microstrip line) are included in the calculation, the Smith-chart takes the form of a spiral. As well known in lossy transmission line theory that, when attenuation as a function of line-length is plotted on the Smith chart, it also takes the form of a spiral.



Fig. 1. The frequency-dependent (lossy) Smith chart with dielectric constant = 5.9 and the size of the microstripstructure from [6] \_\_\_\_\_FDSC

## ..... Standard Smith chart

## III. ICPA AND ITS CIRCUIT MODEL

"Any printed circuit antenna can be used for the ICPA" [3]. The microstrip patch antenna is narrowband and widebeam. Its advantage is that it is relatively inexpensive to manufacture and design especially on UHF band and higher. Consequently, ICPA thermal performance can be augmented by the microstrip patch. Its characteristic is simply modeled as a parallel resonant RLC circuit. To evaluate its characteristics, the calculation based on RLC circuit is most often used.

In this paper, we used the ICPA in the custom designed package format from the previous research as shown in Fig. 2



Fig. 2. ICPA: (a) Top view, (b) cross-section view, and (c) bottom view. (Fig. 2 is from [6])

From Fig. 2, Signal Trace from the carried chip feed the signal to the microstrip patch antenna of the ICPA in the formation of G-S-G bond wires. The corresponding circuit model of the ICPA feeding network is illustrated in Fig. 3. The equivalent RLC can be represented the 5 composites of the ICPA feeding network: the section of microstrip antenna: the section of feeding via underground plane, the section of GSG signal Traces, the section of GSG bond wires, and the section of vias to lands and lands.Next step is the calculation of RLC value in the circuit model of the microstrip patch anetenna. The feeding via that is above the ground plane corresponds with inductive reactance term as shown below [2], [3]

$$XL = \frac{377f_r H}{C_0} ln\left(\frac{C_0}{\pi f_r d_v \sqrt{\varepsilon_r}}\right)$$
(15)

Therefore

 $C_0$  represents velocity of light,

 $d_v$  is diameter of the feeding via,

H represents thickness of the substrate between the microstrip patch and ground plane,

 $\varepsilon_r$  is the relative permittivity of the substrate, and

 $f_r$  is the resonant frequency of the microstrip patch antenna [3].



Fig. 3. Equivalent circuit model of the ICPA feeding network. (Fig. 3 is from [6])

The resonant resistance  $R_a$  of the parallel *RLC* circuit is [3]:

$$R_{a} = \frac{Q_{total} H}{\pi f_{r} \varepsilon_{dyn} \varepsilon_{0} W L_{eff}} \cos 2\left(\frac{\pi X_{eff}}{L_{eff}}\right)$$
(16)

So, length  $L_{eff}$  takes into account the influence of the fringing field at the corners and the dielectric in homogeneity of the ICPA; as a result, the distance from the feeding point to the patch edgeX substituted with

$$X_{eff} = X + \frac{\left(L_{eff} - L\right)}{2} \tag{17}$$

Eq. (16)  $\varepsilon_{dyn}$  signifies the dynamic permittivity, defined as "function of the dimensions of the ICPA and relative permittivity  $\varepsilon_r$  as well as the different modes field distribution"[6]. Calculations of  $\varepsilon_{dyn}$ ,  $C_{e1,stat}(\varepsilon)$  characterize border capacitance on one side of the patch length whereas, *L* and  $C_{e2,stat}(\varepsilon)$  stands for capacitance on one side of a patch with width *W*. More information can be found in [6].

"Therefore, impedance of the dielectric filled microstrip patch of width W "is [3]

$$Za(W) = \frac{\sqrt{\varepsilon_{eff}(W)}}{c_0 C_{tw}(W, H, \varepsilon_r)}$$
(18)

and

$$P_{a}(W) = \frac{2\pi \left[\frac{W}{H} + \frac{W}{(\pi H)}\right] \left[1 + \frac{H}{W}\right]}{\left\{\frac{W}{H} + \frac{2}{\pi} ln \left[2\pi e \left(\frac{W}{2H} + 0.94\right)\right]\right\}^{2}}$$
(19)

Aforementioned,  $f_r$  is the resonant frequency of the microstrip patch antenna where the actual part of the input impedance achieves maximum, the additive reactance, that is X L will not alter value of the resonant frequency

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$$f_r = \frac{c_0}{2\sqrt{\varepsilon_{dyn}}} \sqrt{\left(\frac{m}{W_{eff}}\right)^2 + \left(\frac{n}{L_{eff}}\right)^2}$$
(20)

The effective width  $W_{eff}$  and length  $L_{eff}$  is from [6]. "For the circuit model of feeding via under ground plane,  $L_{v,lower}$ and  $R_{v,lower}$  are the inductance and resistance of the feeding via under ground plane"[3]. The inductance can be derived using the following equation:

$$L_{v,lower} = 20l_{v,lower} \left[ ln\left(\frac{2l_{v,lower}}{r_{v,lower}}\right) - 1 \right] nH$$
(21)

where  $l_{v,lower}$ ,  $r_{v,lower}$  are the length and the radius of the feeding via (in millimeters) under the ground plane

$$R_{v,lower} = \frac{l_{v,lower}}{\sigma S_{v,lower}}$$
(22)

"So,  $l_{v,lower}$ ,  $S_{v,lower}$  and  $\sigma$  are the length, the cross-section area, and the conductivity of the feeding via under the ground plane respectively"[6].

 $C_{v,lower}$  "is the capacitance amidst the feeding via under the ground plane and the ground plane also the shorting vias. It can be derived by the method of moments"[6].

 $C_{sg}$  signifies the capacitance of the signal traces and is a CPW structure. In this study it is derived by the conformal mapping method [6] For circuit model of G-S-G signal traces, [6]

$$C_{sg} = 2\varepsilon_0 \varepsilon_{s,eff} \left[ \frac{K(k_1)}{K(k_1')} + \frac{K(k_0)}{K(k_0')} \right] \times l_8$$
(23)

where  $K(k_i)$  and  $\varepsilon_{s,eff}$  can be found in [6].

The signal trace inductance is derived by [6]

$$L_{sg} = \frac{\mu_0 l_s}{2\pi} \begin{cases} ar \sin h \left( \frac{l_s}{w_s + t} \right) + \frac{l_s}{w_s + t} \\ ar \sin h \left( \frac{w_s + t}{l_s} \right) \\ + \frac{w_s + t}{3l_s} - \frac{1}{3} \left( \frac{l_s}{w_s + t} \right)^2 \\ \left[ \left( \frac{1 + (w_s + t)^2}{l_s^2} \right)^{\frac{3}{2}} - 1 \right] \end{cases}$$
(24)

Hence,  $w_s$  signifies the "width of the signal trace", t is the "thickness of signal trace,"  $l_s$  signifies "length of the signal trace"[6]. In Fig. 3,  $L_{stob}$  and  $L_{stov}$  represents "inductances of the signal trace," which is the length of signal trace to bond wire and signal trace to the via linking the land.

For circuit model of G-S-G bond wires, the inductance and capacitance of the bond wire is [7]:

$$L_{w} = 2l_{w}ln\left(\frac{4h_{w}}{d_{w}}\right)nH$$

$$(25)$$

$$C_{w} = \frac{0.5563l_{w}}{ln\left(\frac{4h_{w}}{d_{w}}\right)}pF$$

$$(26)$$

where  $l_w$ ,  $d_w$  and  $h_w$  are in cm,  $l_w$ ,  $d_w$  and  $h_w$  are the length of the bond wire, the diameter of the bond wire, and the distance from the bond wire to the ground plane [6].

#### IV. RESULTS AND DISCUSSIONS

The modeled and FDSC results are analyzed and a measurement for ICPA is stated from [6]. Referring to the research in [6], the "ICPA designed with Ferro-A6 LTCC material system with dielectric constant of 5.9 and loss tangent of 0.002 at 6 GHz" [6].

The fabricate part of microstrip patch from ICPA which taken from [6]. The ICPA measures  $17 \times 17 \times 1.6$  mm. The top, middle and bottom layers have thickness of .8, 0.4, and 0.4 mm, correspondingly. The vias have diameter of 100 m whereas the traces is the size of  $2 \times 0.4$  mm. The lands are squared with length measured as 0.34 mm. The feeding is 1.2 mm in length whereas vias to the ground plan and lands are 0.4 mm in length. The gap diameter for the feeding via to go through is 0.6 mm. The feeding and grounded bond wires have diameter of 32.5 m and are 0.22mm in length. Illustrated in Fig 1, the dimensions of the microstrip patch antenna are L=9.9 mm, W=15 mm,  $X_0=0.9$  mm,  $Y_0$  1.4 mm, X= 2.35 mm, and Y=7.5 mm. [6]

By applying the FDSC model, the measured and modeled results from are mapped on the frequency-dependent Smith-Chart model in Fig. 1 and then compared with the previous results in [6].



Fig. 4 illustrates the model and measurements of return loss from for the microstrip Patch Antenna in comparison with the FDSC result.

As shown in Fig. 4 the center frequencies of the impedance bandwidth are 5.9, 5.83 and 5.86GHz for the measured [6], modeled, and the FDSC results, respectively. The difference

between the measuresments and model is 0.07GHz (0.07/5.9 = 1.19%), while the difference between the measurements and the FDSC method is only 0.04GHz(0.04/5.9 = 0.68%) as shown in TABLE .

TABLE I: COMPARISON OF THE RETURN LOSS FOR THE ICPA

	Frequency(GHz)	$\Delta\%$
Measured [6]	5.90	-
Modeled[6]	5.83	1.19
FDSC	5.86	0.68



Fig. 5. Comparison of the input impedance for the ICPA.

Fig. 5 shows the measurement and the FDSC input impedance [6]. The resonant frequencies are 5.83, 5.77 and 5.80GHz from the measured model and FDSC results, respectively. The difference between the measured and the modeled [6] is 0.06GHz (0.06/5.83 = 1.03%), while the difference between the measured and FDSC model is only 0.03GHz (0.03/5.83 = 0.51%) as shown in TABLE II:.

TABLE II: RESONANT FREQUENCY				
	Frequency(GHz)	$\Delta\%$		
Measured [6]	5.83	-		
Modeled [6]	5.77	1.03		
FDSC	5.80	0.51		

The resonant resistance of the *RLC* parallel circuit is 89.3 $\Omega$ , 85.45 $\Omega$ , and 87.40 $\Omega$  from the measured, modeled, and FDSC results, respectively. The difference between the measured and modeled is 3.85 $\Omega$  (3.85/87.3 = 4.3%), while the difference between the measured and FDSC is only 1.9 $\Omega$  (1.9/89.3 = 2.1%) as shown in TABLE.

TABLE III:	RESONANT RESISTANCE	
	Ohm(O)	

	$Ohm(\Omega)$	$\Delta\%$
Measured [6]	89.30	-
Modeled [6]	85.45	4.3
FDSC	87.40	2.1

### V. CONCLUDING REMARKS

The use of the frequency-dependent Smith-Chart model is proved to be an accurate method to calculate and model the the frequency-dependent characteristics of microstrip antennas and ICPA applications.

This paper demonstrated a user-friendly and accurate method on verifying existing formulas and measurements.

Overall, the method explained in this research

recommends an effective strategy for portraying the frequency-dependent characteristic of microstrip antennas and ICPA circuit via the FDSC model.

The RF engineers can utilize the FDSC model in this paper to facilitate computer-aided design (CAD) software.

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